

The function **PARTIAL** finds the equivalent partial fraction expansion of the ratio of two polynomials $B(s)/A(s)$.

$$\frac{B(s)}{A(s)} = \frac{r(1)}{s-p(1)} + \frac{r(2)}{s-p(2)} + \dots + \frac{r(n)}{s-p(n)}$$

Vectors B and A specify the coefficients of the numerator and denominator polynomials in descending powers of s .

The function **ROOTS** computes *all the roots* (not like `cZeros`) of the polynomial whose coefficients are the elements of the vector C . If C has $N+1$ components, the polynomial is $c(0)s^N + \dots + c(N)s + c(N+1)$.

Example 1:

$$\frac{B(s)}{A(s)} = \frac{s^2 - 1}{s^3 - 4s^2 - 8}$$

`partial({1, 0, -1}, {1, -4, 0, -8})` give

$$\frac{B(s)}{A(s)} \approx \frac{.1002 + .1932i}{s + .2056 + 1.331i} + \frac{.1002 - .1932i}{s + .2056 - 1.331i} + \frac{.7996}{s - 4.411}$$

Example 2:

$$\frac{B(s)}{A(s)} = \frac{s - 1}{s^3 + s^2}$$

This expression have a pole of multiplicity 2 on $s = 0$

For the expression above (on $A(s)$) `roots({1, 1, 0, 0})` give $\{-1, 0, 0\}$ this is $s = -1$ and $s = 0$ and $s = 0$
 not like `cZeros(s^3 + s^2, s)` who give $\{-1, 0\}$ this is $s = -1$ and $s = 0$
 so the function `partial({1, -1}, {1, 1, 0, 0})` give

$$\frac{B(s)}{A(s)} = \frac{-2}{s+1} + \frac{2}{s} - \frac{1}{s^2}$$

I think these are useful functions.

For example, is much easier to calculate Laplace Transformation. Or in my case, to project digital filters.

24/05/2003

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