

## CROSS-SECTION PROPERTIES

Name of program: **polygon84** V 1.03

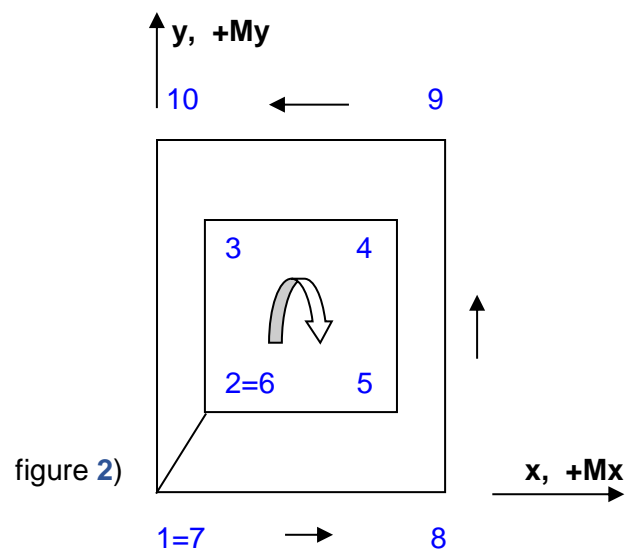
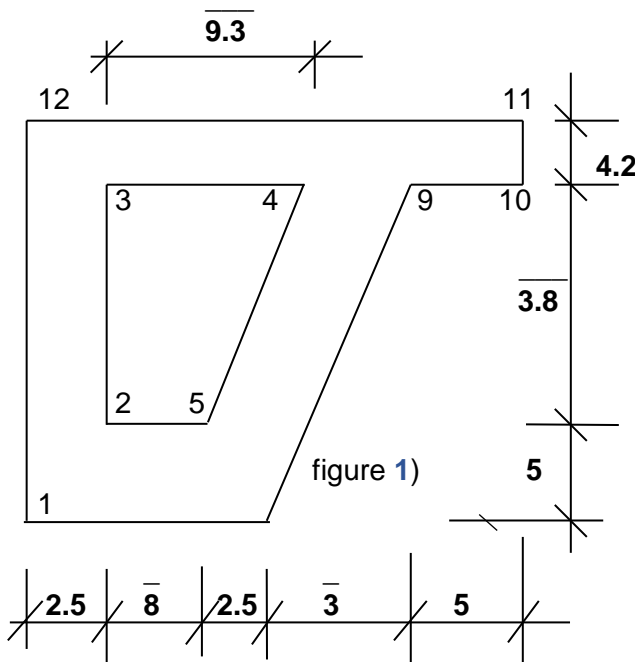
This program determines for a polygonal section the center of gravity, area, moments of inertia and main moments of inertia including the angle of rotation of the main axes.

Furthermore the stresses of all input points may be calculated for any combination of N ( **positive**, if acting as **tension** force ), Mx and My (figure 2). N may be entered as acting in the center of gravity or any point of the section.

Select **POLYGON** and start the program. For a new section, select **1: NEW CONTOUR**, if you have already calculated a system and want to change the loads, select **2: NEW LOADS**. Then key in the NUMBER of points. The display now indicates the number of the point to be entered. Key in xi, yi of all points counterclockwise ( points 7 – 10 in fig. 2 ), missing areas have to be input clockwise ( pts. 2 – 6 ). Make sure that the dimensions of the coordinates are consistent with the loads ( e.g. **cm** and **kNcm** ! ). If all n points are entered, the program prompts for the change of point #i, to offer the opportunity to change points, otherwise enter **0**. The result is indicated as Area **A**, **xs**, **ys** as center point of gravity, moments of inertia **lxs**, **lys**, **lxy** (referred to **xs**, **ys**) and main moments of inertia **I1**, **I2** with angle  $\phi$  of the main axis. After the display of three results the output is halted by **Pause**, so press **enter** to continue. These section quantities are stored in the list variable **L4(1) - L4(9)** !

To end the program here if there are no loads to be examined, enter **0** on the prompt **Calculate  $\sigma_i$ ?**

Following now is the input of N, Mx, My, which results in the display of a plot of the contour including the main axis for I1 and I2 in lightblue as well as the neutral axis, where  $\sigma_F=0$  ( magenta ). Press **stat**, then **1:Edit...** You will find the x-coordinates in list L1, yi in L2, stresses  $\sigma_i$  in L3 and the section properties in L6. L4 and L5 contain the coordinates  $x_0$  and  $y_0$ , where the neutral axis intersects the contour.



**TABLE of COORDINATES ( [cm] ):**

i	xi	yi	i	xi	yi
1	0	0	7	0	0
2	2.5	5	8	13	0
3	2.5	8.8	9	16	8.8
4	11.8	8.8	10	21	8.8
5	10.5	5	11	21	13
6	2.5	5	12	0	13

## EXAMPLE

Being given the section of figure 1) and the loads  $N = -50 \text{ kN}$  acting in the centre of the section;  $M_x = -700 \text{ kNcm}$ , and  $M_y = +200 \text{ kNcm}$ , calculate the stresses  $\sigma_{,i}$  ( $1 \leq i \leq 12$ ).

Select **"POLYGON"**, press **enter** and again **enter**. Select **1: NEW CONTOUR**, then key in **12** for **NUMBER of points** ( fig. 3, fig. 4 )

Now enter the points as indicated in the table. After the 12<sup>th</sup> pair of  $x_i, y_i$  the program offers the opportunity to correct inputs. If you entered a wrong value for point  $i$ , enter now the number  $i$  in the **"CHANGE point #i : "**-field and key in the correct value, otherwise or to exit enter **0**.

```
NORMAL FLOAT AUTO REAL DEGREE MP
SELECT
1:NEW CONTOUR
2:NEW LOADS
```

3)

```
PrgrmPOLYGON
NUMBER of points:12
xi:0
yi:0
xi:2.5
yi:5
xi:
```

4)

```
NORMAL FLOAT AUTO REAL DEGREE MP
A =
xs =
ys =
```

5)

Now the section properties  $A, y_s, z_s, I_{xs}, I_{ys}, I_{yz}, I_1, I_2, \phi$  are displayed (fig. 5 – fig. 7):

```
NORMAL FLOAT AUTO REAL DEGREE MP
Ixs =
Iys =
Ixy =
```

6)

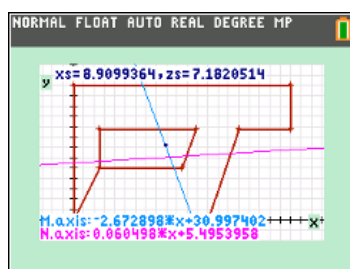
```
NORMAL FLOAT AUTO REAL DEGREE MP
I1 =
I2 =
phi =
```

7)

```
NORMAL FLOAT AUTO REAL DEGREE MP
Calculate sigma? 1
N = -50
xs=S,ys=T
{8.909936406 7.182051422}
x-N =S
y-N =T
Mx(+)= -700
My(+)= 200
```

8)

$A = 182.93$   $xs = 8.9099$   $ys = 7.182$ . Press **enter**:  $I_{xs} = 3010.89$   $I_{ys} = 5739.45$   $I_{xy} = 1186.96$ . Again press **enter**:  $I_1 = 6183.526$   $I_2 = 2566.819$   $\phi = 110.51$ . The next **enter** depicts the contour. After the plot of the contour press **enter**. Program prompts: **Calculate sigma?** Key in **1** ( fig 8.), then enter  $N = -50$ . If  $N \neq 0$ , the input of point  $(x_N, y_N)$ , where  $N$  is acting in, is requested additionally and the program prompts to enter the position of  $N$  on the contour offering  $xs$  and  $ys$ , stored in **S** and **T**. So key in **alpha** **ln** (**=S**) for  $x_N$  and **alpha** **4** (**=T**) for  $y_N$ . Afterwards key in the values of  $M_x = -700$  and  $M_y = 200$ . The following graph displays the contour and the equations of the main axis line **M.axis: -2.6728\*x +30.997**, the neutral axis **N.axis: .0060498\*x+5.49539** and the location and quantities of  $xs=8.9099, ys=7.18205$  ( fig. 9 ).



9)

L1	L2	L3	L4	L5	L6
0	0	1.3088	0	0	
2.5	5	0.154	0	0	
2.5	8.8	-0.751	2.5	5.6466	
11.8	8.8	-0.617	0	0	
10.5	5	0.2693	10.895	6.1545	
2.5	5	0.154	0	0	
0	0	1.3088	0	0	
13	0	1.4961	0	0	
16	8.8	-0.557	15.187	6.4142	
21	8.8	-0.484	0	0	
21	13	1.485	0	0	
L4(5)=10.89496710593					

10)

Press **2nd quit**, then **stat** and **1: Edit...** You will see numerical results stored in  $L_1 - L_6$  ( fig. 10 ):  $L_1$ :  $x_i$  of section points,  $L_2$ :  $y_i$  of section,  $L_3$ : stresses  $\sigma_i$ ,  $L_4$  and  $L_5$ :  $x_0$ , and  $y_0$ , where neutral axis meets contour ( otherwise 0 ). Fig. 10) displays the values  $x_0=10.895$  and  $y_0=6.1545$  between point  $P_4$  and  $P_5$  for  $\sigma_i = 0$ . Finally,  $L_6$  (10) contains the inclination angle  $\gamma$  of the neutral axis ( $= 3.46^\circ$ ). If stress calculation is omitted, this cell contains **0**.

For new loads, start **POLYGON** again, select **2: NEW LOADS** and enter  $N, M_x$  and/or  $M_y$ . In that case **be sure that you have not changed or deleted any variable meanwhile** !

## **HINTS and WARNINGS**

- Pay attention to the applied units! If you enter the coordinates in [**cm**] and moments in [**kNcm**], stresses are output in [**kN/cm<sup>2</sup>**] !
- If all stresses have the same sign, the neutral axis is described by:  
"N.axis: .tan( $\gamma$ )\*x+...,beyond contour!" instead by an equation .

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