

nDerive v2.0 (April 9, 2011)  
by Rob Bradley

Thank you for using this nth derivative solver

The solver operates on the formula:

$$f^{(n)}(x) = \lim_{h \rightarrow 0} \frac{\sum_{i=0}^n (-1)^{n-i} \binom{n}{i} f(x + ih)}{h^n}$$

Derived from the simple derivative formula:

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x + h) - f(x)}{h}$$

The program prompts the user for four (4) inputs:

$f(x)$ , the original function, placed in double quotes (e.g. " $x^2$ ")  
 $x$ , the value of the independent variable of the function  
 $n$ , the nth derivative to find  
 $e$ , epsilon, the level of accuracy involved in dividing very close to, but not at, zero

$h = \pm 10^{-e}$ , where  $e$  is the level of accuracy and  $h$  is the approximation of the infinitesimal distance  
 $x_n - x_{n-1}$

Because we cannot divide by zero, the program compares the derivatives from both sides as the limits approach zero

Right side:

$$f^{(n)}(x) = \lim_{h \rightarrow 0^+} \frac{\sum_{i=0}^n (-1)^{n-i} \binom{n}{i} f(x + ih)}{h^n}, h > 0$$

Left side:

$$f^{(n)}(x) = \lim_{h \rightarrow 0^-} \frac{\sum_{i=0}^n (-1)^{n-i} \binom{n}{i} f(x + ih)}{h^n}, h < 0$$

Known bugs:

-Returning zero (0) for the derivative of some functions with infinite derivatives (e.g. " $e^x$ ") if the level of accuracy is too high

-Divide by zero errors if the level of accuracy is too high

-Accuracy is not guaranteed

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